

Q.1 Solve the equation.

(A) $\left(\frac{3}{7}\right)^{2x-7} = \left(\frac{7}{3}\right)^{7x-2}$

(P) $x = -1$

(B) $9^x + 6^x = 2 \cdot 4^x$

(Q) $x = 0$

(C) $5^{x+1} - 5^{x-1} = 24$

(R) $x = 1$

(D) $6^x + 6^{x+1} = 2^x + 2^{x+1} + 2^{x+2}$

(S) $x = 2$

[Ans. (A) R, (B) Q, (C) R, (D) Q]

[2+2+2+2+2+2=12]

Q.2

Column-I

Column-II

(A) If $a = 3\left(\sqrt{8+2\sqrt{7}} - \sqrt{8-2\sqrt{7}}\right)$, $b = \sqrt{(42)(30)+36}$, then the value of $\log_a b$ is equal to

(P) -1

(B) If $a = \sqrt{4+2\sqrt{3}} - \sqrt{4-2\sqrt{3}}$, $b = \sqrt{11+6\sqrt{2}} - \sqrt{11-6\sqrt{2}}$, then the value of $\log_a b$ is equal to

(Q) 1

(C) $a = \sqrt{3+2\sqrt{2}}$, $b = \sqrt{3-2\sqrt{2}}$, then the value of $\log_a b$ is equal to

(R) 2

(D) $a = \sqrt{7+\sqrt{7^2-1}}$, $b = \sqrt{7-\sqrt{7^2-1}}$, then the value of $\log_a b$ is equal to

(S) $\frac{3}{2}$

(E) The number of zeroes at the end of the product of first 20 prime numbers, is (T) None

(F) The number of solutions of $2^{2x} - 3^{2y} = 55$, in which x and y are integers, is

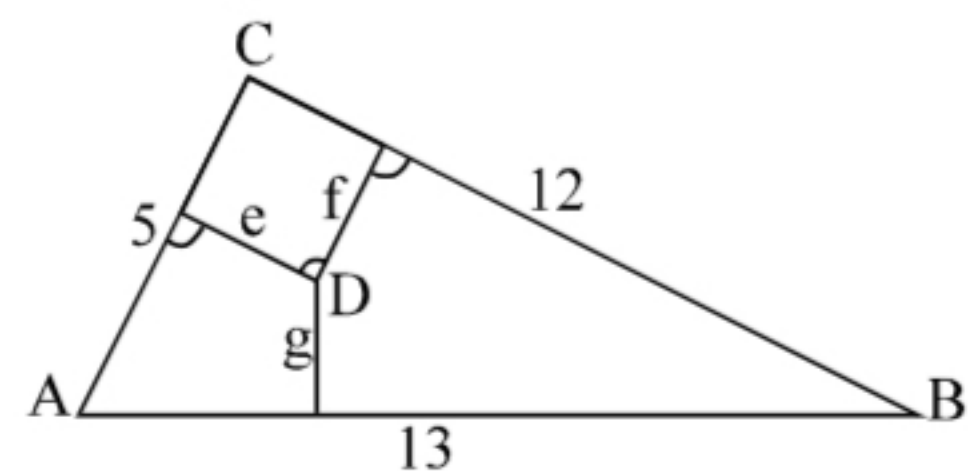
[Ans. (A) R; (B) S; (C) P; (D) P; (E) Q; (F) Q]

[INTEGER TYPE / SUBJECTIVE]

Q.3 The sides of a triangle ABC are as shown in the given figure. Let D be any internal point of this triangle and let e, f, and g denote the distance between the point D and the sides of the triangle. Find the sum $(5e + 12f + 13g)$.

[4]

[Ans. 60]



Q.4 An equilateral triangle and a regular hexagon have the same perimeter, find the ratio of their areas. [4]

[Ans: 2 : 3]

Q.5 Establish tricotomy in each of this following pairs of numbers

[4]

(i) $3^{\log_{27} 3}$ and $2^{\log_4 2}$

(ii) $\log_4 5$ and $\log_{1/16} (1/25)$

(iii) 4 and $\log_3 10 + \log_{10} 81$

(iv) $\log_{1/5} (1/7)$ and $\log_{1/7} (1/5)$

[Ans. (i) (Hint: >); (ii) (Hint: =); (iii) (Hint: <); (iv) (Hint: >)]

Q.6 Compute the value of $81^{\frac{1}{\log_5 3}} + 27^{\log_9 36} + 3^{\frac{4}{\log_7 9}}$

[4]

[Ans. 890]